# Tests of chiral perturbation theory in $\mathbf{K}_{\mathrm{S}}$ rare decays at NA48

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Received: 15 October 2003 / Accepted: 12 November 2003 / Published Online: 1 December 2003 – © Springer-Verlag / Società Italiana di Fisica 2003

**Abstract.** The NA48 collaboration has performed an extensive study of rare kaon decays. In particular tests of Chiral Perturbation Theory have been done, using data from the  $\text{Re}(\varepsilon'/\varepsilon)$  runs in 1998 and 1999 for  $K_L \rightarrow \pi^0 \gamma \gamma$  and from the NA48/1 High Intensity  $K_S$  for  $K_S \rightarrow \gamma \gamma$  and for the first observation of  $K_S \rightarrow \pi^0 \gamma \gamma$ 

**PACS.** 13.20.Eb Decays of K mesons – 14.40.Aq  $\pi$ , K and  $\eta$  mesons

### 1 Introduction

The program of NA48 included, apart from the measurement of  $\operatorname{Re}(\varepsilon'/\varepsilon)$ , an extensive study of rare kaon decays. Data collected in the 1999  $\operatorname{Re}(\varepsilon'/\varepsilon)$  run were used to study a number of  $K_L$  rare decays. A 40 hours test run in 1999 using a  $K_S$  only beam with 200 times the standard  $\operatorname{Re}(\varepsilon'/\varepsilon)$   $K_S$  intensity was performed to demonstrate the feasibility of a high intensity  $K_S$  program. A specific proposal (NA48/1) was approved and high intensity  $K_S$ data were collected in 2000 and 2002. Specific information on the setup used for the 2000 run, relevant for the results presented here, can be found in [1]. Among the processes studied, we report here results on the radiative nonleptonic decays  $K_L \to \pi^0 \gamma \gamma$ ,  $K_S \to \gamma \gamma$  and  $K_S \to \pi^0 \gamma \gamma$ .

### 2 Study of the decay ${ m K_L} o \pi^0 \gamma \gamma$

 $K_L \rightarrow \pi^0 \gamma \gamma$  decay is important because the decay rate prediction from  $O(p^4) \chi PT$  is finite, but 2-3 times smaller than the measured one [2]. Going to  $O(p^6)$  and including vector meson exchange, the measured rate is reproduced and a tail at low  $m_{\gamma\gamma}$  is predicted. The vector meson dominance contribution is parametrized by  $a_v$ , to be measured, and the low  $m_{\gamma\gamma}$  tail determines the CPC amplitude to the decay  $K_L \rightarrow \pi^0 e^+ e^-$ . Predictions from  $\chi PT$ are  $BR(K_L \rightarrow \pi^0 \gamma \gamma) = 1.5 \ 10^{-6}$  and  $a_v = -0.7$ .

Data from 1998 and 1999 runs were selected using the same trigger as the  $K_L \rightarrow \pi^0 \pi^0$  mode, which has been used as normalization channel. In this way many systematic uncertainties cancel out.

The background from  $K_L \rightarrow \pi^0 \pi^0$  is rejected using invariant mass cuts: one pair of photons should be within 3 MeV from the pion mass, while the other should be outside the 110 MeV-160 MeV window. Transverse momentum of

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the lowest energy unpaired photon should be greater than 40 MeV/c.

The background from  $K_L \rightarrow 3\pi^0$  with missing or overlapping photons is rejected on a basis of a variable  $(z_{max})$ designed to estimate the true kaon decay position, assuming a  $3\pi^0$  decay. This estimate applied to signal events produces an unphysical result with a distribution mainly populated in the region upstream of the final collimator. The condition  $z_{max} < -5m$  rejects  $\approx 99\%$  of the  $3\pi^0$  background, keeping 46% of the signal.



Fig. 1.  $K_L \rightarrow \pi^0 \gamma \gamma$ : Background rejection



Fig. 2.  $K_L \to \pi^0 \gamma \gamma$ : Events in the signal region and  $m_{\gamma\gamma}$  distribution

 $\approx 2500$  events were found in the signal region (132 MeV < M<sub> $\pi^0$ </sub> < 138 MeV) [3]. Fitting the M<sub> $\gamma\gamma$ </sub> distribution, one obtains

$$\mathbf{a}_v = -0.46 \pm 0.03_{st} \pm 0.03_{sy} \pm 0.02_{th}$$

Using the fitted  $a_v$  value, the branching ratio is

$$BR(K_{L} \to \pi^{0} \gamma \gamma) = (1.36 \pm 0.03_{st} \pm 0.03_{sy} \pm 0.03_{norm}) \cdot 10^{-6}.$$

and the CP conserving part of the  $K_L \rightarrow \pi^0 e^+ e^-$  decay is

$$BR(K_L \to \pi^0 e^+ e^-)_{CPC} = (4.7 \pm 2.2) \cdot 10^{-13}$$

#### 3 Study of the decay ${ m K_S} ightarrow \gamma\gamma$

 $K_S \rightarrow \gamma \gamma$  is interesting because it is calculable in O(p<sup>4</sup>)  $\chi PT$  with no counterterms and it is sensitive to loops [4,5,6]. The theoretical prediction for the BR is (2.1 ± 0.2)·10<sup>-6</sup>. NA31 measured [7]

$$BR(K_S \rightarrow \gamma \gamma) = (2.4 \pm 0.9) \cdot 10^{-6}$$

With the data from the 1999 HIKs run with a dedicated trigger, NA48 has published [8]

$$BR(K_S \to \gamma \gamma) = (2.58 \pm 0.36_{st} \pm 0.22_{sy}) \cdot 10^{-6}$$

A better measurement has been performed using data from the 2000 run. The normalisation channel is  $K_S \rightarrow \pi^0 \pi^0$ .

The  $K_S \rightarrow \pi^0 \pi^0$  background is minimized using a 5 meter fiducial region after the  $K_S$  collimator. These decays with two lost  $\gamma$  have a maximum invariant mass of 458 MeV and the reconstructed vertex cannot be less than 9 meters. This number is reduced to 5 meters because of the effect of overlapping showers. Hadronic interactions in the collimator and accidental  $\gamma\gamma$  pairs are eliminated with suitable cuts.

The background from  $K_L \rightarrow \gamma \gamma$  is instead irreducible and it amounts to 1.5 times the  $K_S$  channel. The subtraction of this background is done evaluating the  $K_L$  flux using  $K_L \rightarrow 3\pi^0$  and measuring  $\Gamma(K_L \rightarrow \gamma \gamma)/\Gamma(K_L \rightarrow 3\pi^0)$ using the data from the far target run with  $K_L$  only. For this measurement the detector conditions are similar to the  $K_S$  data taking, so detector systematics cancel. The decay volume is the same as for  $K_S \rightarrow \gamma \gamma$  and the acceptance differences almost cancel. After subtracting hadronic background and evaluating the systematic uncertainties due to acceptance and background subtraction, we obtain an independent measurement:

$$\Gamma(\mathrm{K_L} \to \gamma\gamma)/\Gamma(\mathrm{K_L} \to 3\pi^0) = (2.81 \pm 0.01_{st} \pm 0.02_{sy}) \cdot 10^{-3}$$

The total number of  $K_{S,L} \rightarrow \gamma \gamma$  is 19916. The global systematic correction is -1.8 ± 1.4 %. Statistical errors on data and on the Montecarlo sample are respectively 2.0% and 0.6%.

The result is

$$BR(K_S \to \gamma \gamma) = (2.78 \pm 0.06_{st} \pm 0.03_{sy} \pm 0.02_{ext}) \cdot 10^{-6}$$

This result is compatible with previous measurements, but it shows a 30% difference wrt to  $O(p^4) \chi PT$  predictions, indicating a possible large  $O(p^6)$  contribution.





Fig. 4.  $K_S \rightarrow \gamma \gamma$ : Theoretical predictions and measured values

# 4 First observation of $K_S \to \pi^0 \gamma \gamma$

The study of  $K_{\rm S} \to \pi^0 \gamma \gamma$ , as in other radiative nonleptonic kaon decays, is useful to check  $\chi \rm PT$  predictions for the low energy hadron dynamics. In the decay  $K_{\rm S} \to \pi^0 \gamma \gamma$  the photon pair is produced by a pseudo-scalar meson. A measurement of the branching ratio can give information on possible extra non-pole contributions [9]. The prediction for the branching ratio is limited to the kinematical region  $z = m_{\gamma\gamma}^2/m_K^2 > 0.2$  and it is  $3.8 \times 10^{-8}$  [10]. Additional information from the z spectrum can determine, if sufficient statistics is available, the momentum dependence of the weak vertex.

Using data from the 1999  $K_S$  run, NA48 has published [11] the upper limit

$$BR(K_S \to \pi^0 \gamma \gamma)_{z>0.2} < 3.3 \cdot 10^{-7}$$

at 90% confidence level.

Data has been collected in the 2000 run using the same trigger for  $K_S \rightarrow \pi^0 \pi^0$  and  $K_S \rightarrow \pi^0 \gamma \gamma$ , so that many systematic uncertanties cancel out.

The selection for  $K_{\rm S} \to \pi^0 \gamma \gamma$  requires the two best matching photons with the  $\pi^0$  mass, while the others should have  $m_{\gamma\gamma}^2/m_K^2 > 0.2$ . Cuts on a  $\chi^2$  variable built with the sums and differences of the  $\gamma\gamma$  pair masses and their resolutions discriminate between  $K_{\rm S} \to \pi^0 \pi^0$  and  $K_{\rm S} \to \pi^0 \gamma \gamma$ .

The large background from  $K_S \to \pi^0 \pi_D^0$  with one photon out of the acceptance is reduced with a cut on the z coordinate of the decay point between -1m and 8m. Most of the background from  $K_S \to \pi^0 \pi_D^0$  and even more from  $K_L \to 3\pi^0$  is reconstructed downstream of this region because of the missing energy. Further suppression of  $K_S \to \pi^0 \pi_D^0$  background is achieved imposing cuts on the closest  $z_{\pi^0}$  to the collimator, where  $z_{\pi^0}$  are the vertex positions of  $\gamma\gamma$  pairs.

Irreducible background from  $K_L \rightarrow \pi^0 \gamma \gamma$  is estimated from the  $K_S \rightarrow \pi^0 \pi^0$  rate, assuming equal  $K_S$  and  $K_L$  production at the target. Residual background from  $\Xi^0 \rightarrow \Lambda^0 \pi^0$  with  $\Lambda^0 \rightarrow n\pi^0$  with one  $\gamma$  escaping and with a narrow n shower is suppressed rejecting asymmetric topologies. Accidental pile-up background is reduced with tight cuts on the shower times, which should be within 1 nsec.

After the selection the final sample consists of 31 events. The normalization sample of about  $285 \cdot 10^3$  has been used. The background estimation is  $13.7 \pm 3.2$  events of which the half is due to pile-up accidentals. The probability of observing in the signal region 31 or more events when the background is  $13.7 \pm 3.2$  is  $1.5 \cdot 10^{-3}$ . In the control region the data agree with the background estimate.  $17.3 \pm 6.4$  signal events are obtained after background subtraction. Acceptances were computed using a Monte Carlo simulation and are 18.6% for  $K_S \rightarrow \pi^0 \pi^0$  and  $7.2 \pm 0.3\%$  for  $K_S \rightarrow \pi^0 \gamma \gamma$ .

Normalising to  $K_S \rightarrow \pi^0 \pi^0$  with the proper ratio of acceptances gives

$$\Gamma(\mathrm{K}_{\mathrm{S}} \to \pi^{0} \gamma \gamma)_{z>0.2} / \Gamma(\mathrm{K}_{\mathrm{S}} \to \pi^{0} \pi^{0}) = (1.57 \pm 0.51_{st} \pm 0.29_{sy}) \cdot 10^{-7}$$

The result is stable against variation of the most relevant cuts. Using  $BR(K_S \rightarrow \pi^0 \pi^0)$  from PDG one obtains

$$BR(K_{\rm S} \to \pi^0 \gamma \gamma)_{z>0.2} = (4.9 \pm 1.6_{st} \pm 0.9_{sy}) \cdot 10^{-8} = (4.9 \pm 1.8) \cdot 10^{-8}$$

in agreement with [10].

The z distribution of the events after background subtraction has been compared with z distributions of simulated events using two different decay generators, one with  $\chi$ PT matrix element and the other with pure phase space. The experimental data agree with both calculations and none of the two predictions can be preferred.



Fig. 5.  $K_S \rightarrow \pi^0 \gamma \gamma$ : Data and background distribution



Fig. 6.  $K_S \rightarrow \pi^0 \gamma \gamma$ :  $z_q$  distribution for data and two theoretical models

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